

Name: SOLUTIONS

Section 1.7 - In class example

Math 151 - Spring 2018

1. Find the present value of an \$8000 payment to be made in 5 years.

4% compounded continuously

Recall that in this case

$$P = \frac{\$8000}{e^{0.04(5)}} = \$6,549.84.$$

2. 4000 dollars is invested in a bank account at an interest rate of 8% per year, compounded continuously. Meanwhile, 20000 dollars is invested in a bank account at an interest rate of 3 percent compounded annually. When will the two accounts have the same balance?

We want to find t such that:

Account 1

Account 2

$$4000 e^{0.08t} = 20,000 (1+0.03)^t = 20,000 (1.03)^t$$

Indeed,

$$\frac{4000 e^{0.08t}}{4,000} = \frac{20,000 (1.03)^t}{4,000}$$

$$e^{0.08t} = 5 (1.03)^t$$

$$\ln(e^{0.08t}) = \ln(5 \cdot (1.03)^t)$$

$$0.08t = \ln(5) + \ln(1.03)^t$$

* using $\ln(AB) = \ln(A) + \ln(B)$

$$0.08t = \ln(5) + t \ln(1.03)$$

$$(0.08 - \ln(1.03))t = \ln(5)$$

$$t = \frac{\ln(5)}{0.08 - \ln(1.03)}$$