Exercise 1: Matrix and Array manipulations

- 1. Let vec = [4 5 9 6]
 - (a) Subtract 3 from each element
 - (b) Add 11 to the odd-index elements
 - (c) Compute the square root of each element
 - (d) Raise to the power of 3 each element.
- 2. Create a vector **v** with elements $v_n = \frac{(-1)^n}{2n-1}$ for n = 1, 2, 3, ..., N for any N. Find the sum of the 100-element vector. Hints:
 - start with the vector of all -1s and perform the appropriate element-wise operations
 - Use the MATLAB sum command
- 3. Given a vector t, write down MATLAB expressions that will compute (componentwise)
 - (a) $\ln(2+t+t^2)$ (b) $\frac{1}{1+t^2}$

Test you code with any vector t of your choice.

4. Recall that the angle between non-zero vectors \boldsymbol{u} and \boldsymbol{v} is given by

$$\cos \theta = rac{oldsymbol{u} \cdot oldsymbol{v}}{|oldsymbol{u}||oldsymbol{v}|}$$

where $|\boldsymbol{v}|$ is the Euclidean *norm* of the vector \boldsymbol{v} . Use Matlab to calculate the angle between $\langle 2, 2, -1 \rangle$ and $\langle 5, -3, 2 \rangle$.

- 5. Given the vectors $\mathbf{x} = \begin{bmatrix} 1 & 3 & 7 \end{bmatrix}$ and $\mathbf{y} = \begin{bmatrix} 2 & 4 & 2 \end{bmatrix}$ and matrices $\mathbf{A} = \begin{bmatrix} 3 & 1 & 6; & 5 & 2 & 7 \end{bmatrix}$ and $\mathbf{B} = \begin{bmatrix} 1 & 4; & 7 & 8; & 2 & 2 \end{bmatrix}$, determine which of the following statements can be correctly executed in MATLAB. In each case explain *briefly* what the operation does or why MATLAB yields an error message.
 - x + y
 - x + A
 - x' +y
 - A [x' y']
 - [x; y']
 - B*A
 - A.*B
 - A'.*B
 - B./x'

- ones(1,3)*A
- 4./B

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- [A, fliplr(A)]
- B(3,4) = 2;
- 6. The MATLAB \land operator can be used to solve linear systems. Let A be a random 5×5 matrix and b be a random 5×1 vector. Given Ax = b find x by calling $\mathbf{x} = \mathbf{A} \setminus \mathbf{b}$, compare your result to using MATLAB's inv operator. Having found \mathbf{x} , check whether Ax - b is close to zero.
- 7. The MATLAB magic function returns a square matrix whose row sums, column sums and the sums of the two diagonals are the same. Consider the matrix

A = magic(201); % do not print the entries

The matrix **A** has 201 row sums and 201 column sums, and two diagonal sums. These 404 sums should be exactly the same, and you **could** verify this by printing them and checking visually but it is easy to miss a digit with so many numbers. **Instead**, verify that A is a magic square by constructing 201 column sums (without printing them) and computing the maximum and minimum values of the column sums. Do the same for the 201 row sums, and compute the two diagonal sums. Check that the six values are the same. If the maximum and minimum values are the same, then this confirms that the row, diagonal and column sums are the same. **Hints:**

- Use the MATLAB functions min and max
- Use >>help sum to determine the result of calling sum(X) where X is a matrix or vector.
- The Matlab diag function extracts the diagonal of a matrix, you can extract the other diagonal by calling diag(fliplr(A))
- 8. In the following exercise, use the provided loyola.jpg or any colorful image of your choice. Define a 3D matrix Img storing the RGB values and view the image you have loaded as follows:

```
1 Img = imread('loyola.jpg');
2 imshow(Img);
3 %enable viewing of RGB values
4 datacursormode('on')
```

Notice that if you click on your image, you can view the corresponding red, blue and green values at each position.

- (a) Confirm that Img is a 3D matrix
- (b) Create a new image (ex1_prob8b.jpg) that consists of the original image and its reflection as shown in Figure 1.
- (c) Loyola's official green color has RGB values 0, 104 and 87. Create a framed image (ex1_prob8c.jpg) that is 10 pixels wide in each direction by overriding the image at the boundary as shown in Figure 2.



Figure 1: Composite Image





- (d) Convert the color image to grey-scale by manipulating the 3D matrix as follows
 - i. Create a new 2D matrix BW1 that consists of the average of the RGB values at each point. Use imshow(BW1) to view your new image, save it as ex1_prob8d_bw1.jpg.
 - ii. Create a new 2D matrix BW2 using a weighted average of the RGB values as follows

BW2 = 0.21 R + 0.72 G + 0.07 B

Save your image as ex1_prob8d_bw2.jpg.

iii. Finally create BW3 by averaging the maximum and minimum values at each point as BW3 = (min(R,G,B) + max(R,G,B))/2

and save your image as ex1_prob8d_bw3.jpg.

(e) Which black and white image do you prefer? Explain.

Exercise 2: Plotting

For each of these plots label your jpg file as ex2_probN_part.jpg if the problem has multiple parts.

- 1. Look up the MATLAB function polarplot and use it to plot the polar curve $r = 1 + \sin(8\theta)$ for $0 \le \theta \le 2\pi$.
- 2. Consider the function $f(x) = \frac{1}{3}x^4 8x^2 + 4x + 1$ for $-10 \le x \le 10$.
 - (a) Find the first and second derivatives of f and include them in your summary file.
 - (b) Plot y = f(x), y = f'(x), y = f''(x) on the same graph. Make sure to include a title and descriptive legend and use different colors and line styles for each function.
- 3. Plot the following 3D surfaces, for each specify the problem number and part
 - (a) $z = x^3 3xy^2, x, y \in [-15, 15] \times [-15, 15]$ Use mesh
 - (b) $z = \frac{\sin(x^2 + y^2)}{x^2 + y^2}$ on $x, y \in [-5, 5] \times [-5, 5]$. Use surf and let the z-axis go from -2 to 2. Note: you can change the z-axis by specifying the limits as $zlim([-2 \ 2])$.
- 4. Plot the level curves of $f(x, y) = -150xye^{-x^2-y^2}$ on $[-4, 4]^2$ using contour(X,Y,Z) where X,Y are matrices consisting of the x and y coordinates and function values in the matrix Z
- 5. Plot paraboloid $z = 2x^2 + y^2$ and the tangent plane z = 4x + 2y 3 on $[-4, 4]^2$ on the same graph. Note: you can modify the edge of face color by specifying options for 'FaceColor' and 'EdgeColor' in your calls to surf and make sure to use the option axis equal to ensure the correct perspective.
- 6. Pick your favorite function f. Use subplot to illustrate on a 2×2 grid, the function f and 3 transformations of your choice.

Submission of exercises

Place all your files (m-files, summary.txt, diary.txt) in a folder named lastname_hwN and zip the folder to create a file lastname_hwN.zip. Email your zip file lastname_hwN.zip to pchidyagwai@loyola.edu with subject MA302_hwN.