Instructions:

The code submitted should be your own creation. You may consult MATLAB's documentation or the notes from class. The submission of codes obtained from online sources is a violation of Loyola's honor code.

Exercise 1: Linear Transformations

Download the provided script linear_trans.m. Provide MATLAB commands to visualize the following transformations. In each case use the MATLAB command saveas(gcf,'prob1_ex1.jpg') to save the image visualizing problem 1 exercise 1, for example. Your figures should contain a title describing the transformation and axis labels. Your plot should include both the original and transformed shapes. Write a small script for each problem.

- 1. Rotation by an angle $\theta = \frac{\pi}{8}$
- 2. Reflection along the x-axis.
- 3. A random orthogonal transformation. Mark two reference points and show how the orthogonal transformation modifies them.
- 4. A translation along the vector \mathtt{v} =[3,0] and then a dilation by a factor of 2
- 5. Write a script that animates the following sequence of 2000 transformations. **Implementation notes:**
 - (a) Use the commands

to open the movie file mymovie.avi

(b) In a loop that runs from k = 1 to 2000, for the shape provided in linear_trans.m, rotate by 1 degree in an anti-clockwise direction and scale the image by a factor of c = 0.999 and for values of k <= 1000 and for values of k > 1000, rotate by 1 degree in a clockwise direction dilate the shape by c = 1.001. For each iteration, plot the transformed image using connect_dots with an axis size of 5 and save the movie frames for the animation using the commands

```
frame = getframe(gcf);
writeVideo(v,frame);
```

- (c) After exiting the loop call close(v) to finish writing the animation.
- (d) Your current directory should contain a file 'mymovie.avi', check to make sure it works.
- 6. Add your own non-trivial twist to the animation and save that in a file 'mymovie2.avi'.

Exercise 2: Fractals

1. Write a MATLAB function fern_generator.m that implements the following affine transformations N iterations to generate a figure of a fern fractal. Your function should return the amount of time it takes for the fractal to be plotted. On each iteration, each transformation is picked at random following the following probabilities:

(a) 85% of the time:

$$T_1 = A_1 \vec{v} + \vec{b}_1 = \begin{bmatrix} 0.85 & 0.04 \\ -0.04 & 0.85 \end{bmatrix} \vec{v} + \begin{bmatrix} 0 \\ 1.6 \end{bmatrix}$$

(b) 7% of the time:

$$\boldsymbol{T}_2 = \boldsymbol{A}_2 \vec{v} + \vec{b}_2 = \begin{bmatrix} 0.20 & -0.26\\ 0.23 & 0.22 \end{bmatrix} \vec{v} + \begin{bmatrix} 0\\ 1.6 \end{bmatrix}$$

(c) 7% of the time:

$$\boldsymbol{T}_{3} = \boldsymbol{A}_{3}\vec{v} + \vec{b}_{3} = \begin{bmatrix} -0.15 & 0.28\\ 0.26 & 0.24 \end{bmatrix} \vec{v} + \begin{bmatrix} 0\\ 0.44 \end{bmatrix}$$

(d) 1% of the time:

$$\boldsymbol{T}_4 = \boldsymbol{A}_4 \vec{v} = \begin{bmatrix} 0 & 0 \\ 0 & 0.16 \end{bmatrix} \vec{v}$$

Implementation notes:

- (a) For each iteration, use the MATLAB function randsample (see class notes for usage) to pick a random integer corresponding to T_i , $i = 1 \cdots 4$ with the given probabilities.
- (b) Construct a switch statement to execute the transformation corresponding to the output from randsample. Plot each point after the transformation.
- (c) Use the MATLAB functions tic and toc to time your iterations.
- (d) Use plot with 'MarkerSize' of 2.5 to plot each point.
- (e) You do not need to have separate colors for each transformations.

Testing

Run your code for N = 5000, 25000 and 50000. Provide the CPU times and plots of the fern for each value of N.

- 2. Write a new function fern_generator_optimized.m that speeds up the computations above in the following way:
 - (a) Preallocate memory for a matrix to store all the points computed from the iterations using the MATLAB function zeros
 - (b) Plot all the points at once after completing the iteration.

Run your code for N = 5000, 25000, 50000 and provide the CPU times in your summary file.

Submission of exercises

Place all your files (m-files, image, movie, summary.txt, diary.txt) in a folder named lastname_hwN and zip the folder to create a file lastname_hwN.zip. Email your zip file lastname_hwN.zip to pchidyagwai@loyola. with subject MA302_hwN.