## Worksheet 03/27

## To do List

1. Watch videos on the Introduction to the Variation of Parameters, the general case and the Example and make detailed notes.
2. Attempt the problems below
3. NOTE: I will not collect the worksheet problems. These problems are meant to check your understanding and generate questions to ask me during office hours if you get stuck.

## Objectives

By the end of this lecture you should be able to

1. Use the variation of parameters technique to solve second order problems with a right hand side that does not fit into categories of the method of undetermined coefficients.

Find the general solution for

1. $y^{\prime \prime}-2 y^{\prime}+y=\frac{e^{t}}{1+t^{2}}$ Your solution should be:

$$
y(t)=c_{1} e^{t}+c_{2} t e^{t}-\frac{1}{2} e^{t} \ln \left(1+t^{2}\right)+t e^{t} \arctan (t)
$$

2. $4 y^{\prime \prime}+y=2 \sec (t / 2),-\pi<t<\pi$ Your solution should be:

$$
y(t)=c_{1} \cos (t / 2)+c_{2} \sin (t / 2)+2 \cos (t / 2) \ln (\cos (t / 2))+t \sin (t / 2)
$$

## Additional Reading/ Examples

Section 3.6 pages 142-143 (Example 1)

