Math 251: Pledged Set 2

Due: January 26, 2010

This is a pledged set. Therefore, no outside help from book, calculator, or other people.

- 1. Suppose an object moves along a curve with position f(t) at time t. Write an expression for the instantaneous velocity of the object at time t = a. How can you interpret this velocity in terms of the graph of f?
- 2. Explain what it means to say

$$\lim_{x \to 1^{-}} f(x) = 2$$
 and $\lim_{x \to 1^{+}} f(x) = 4$

In this situation is it possible that $\lim_{x\to 1} f(x)$ exists? Explain.

3. Evaluate the limit

$$\lim_{x \to 2} \frac{2x^2 + 1}{x^2 + 6x - 4}$$

4. Evaluate (if it exists)

$$\lim_{x \to -4} \frac{\sqrt{x^2 + 9} - 5}{x + 4}$$

5. Prove using the ϵ, δ definition that

$$\lim_{x \to 2} (14 - 5x) = 4$$